

Steve, our mentor



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Steve's students

- **Kent Blackburn (1990)**

Senior Resesarch Scientist (MPS)

LIGO Laboratory, Caltech, Pasadena, California, USA

- **Brian Baker (2002)**

Principal Systems Engineer

Ball Aerospace, Boulder, Colorado, USA

- **Dong-Hoon Kim (2005)**

Researcher

Institute for the Early Universe, Ewha Women's University, Seoul, Rep of Korea

- **Ian Vega (2009)**

Associate Professor

University of the Philippines, Diliman, Philippines

Then ...

$$\nabla^2 \psi = -4 \pi \rho.$$

$$\nabla_{(0+1+2)}^2 \bar{h}_{S ab}^{(0+1+2)} + 2R_{(0+1+2) a b}{}^{c d} \bar{h}_{S cd}^{(0+1+2)} = -16\pi T_{ab}$$

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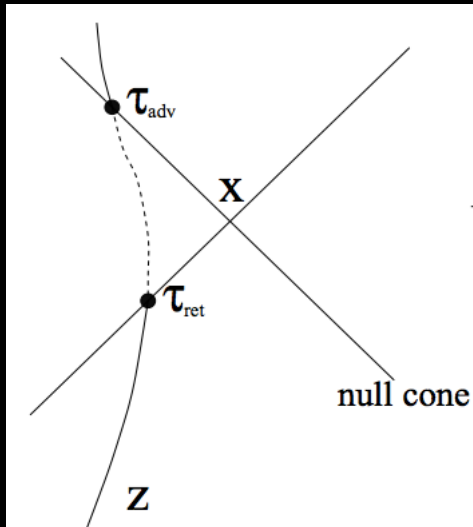
Analytical solutions
Numerical solutions

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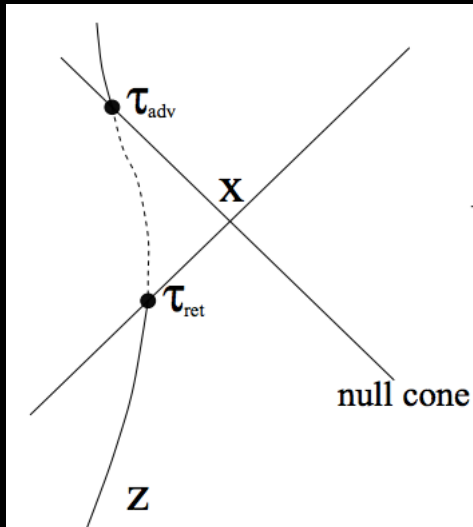


Then and Now

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Analytical solutions
Numerical solutions



$$\vec{\nabla} \cdot (\rho \vec{v}) = S_B$$

$$\frac{\rho}{\varepsilon} \left[\frac{\partial \vec{v}}{\partial t} + \varepsilon^{-1} (\vec{v} \cdot \vec{\nabla}) \vec{v} \right] = -\vec{\nabla} p - \mathfrak{K}_c^{-1}(\vec{x}) \vec{v}$$

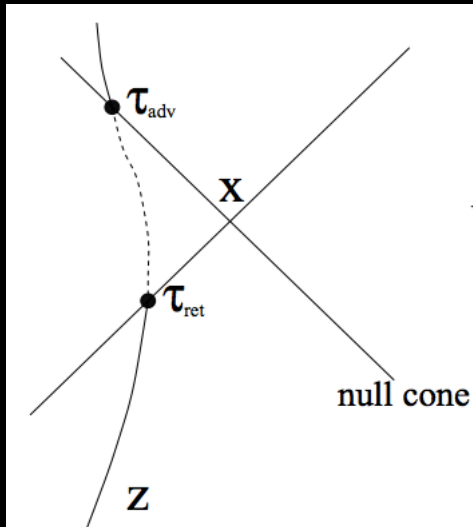
$$\phi \frac{\partial c}{\partial t} + \nabla \cdot (\mathbf{v}c) = \nabla \cdot (\phi \mathbf{D}_t \cdot \nabla c)$$

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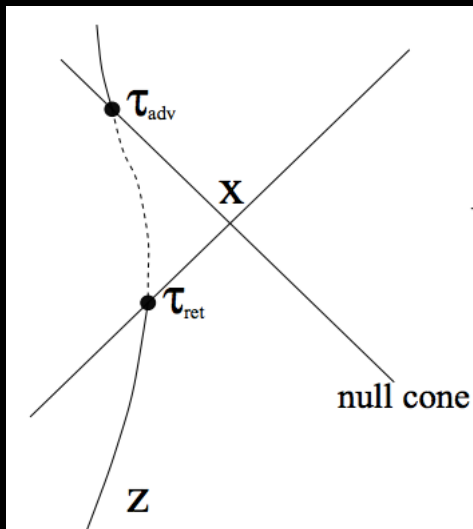
Numerical solutions

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Analytical solutions
Numerical solutions

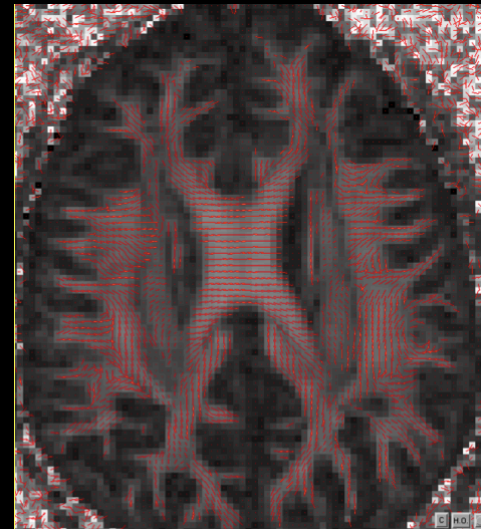


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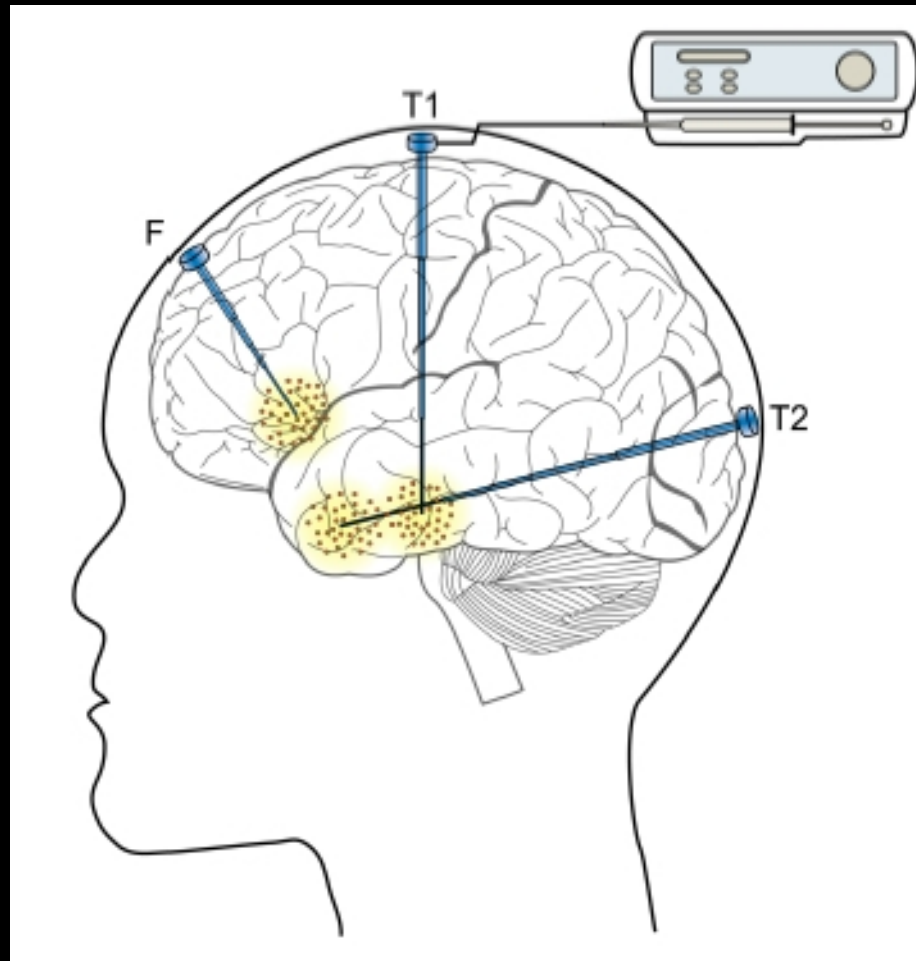
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Numerical solutions



Delivery of medicine to the brain

Delivery of medicine to the brain



Fluid Dynamics Equations

- Mass balance

$$\vec{\nabla} \cdot (\rho \vec{v}) = S_B$$

- Momentum balance

$$\frac{\rho}{\varepsilon} \left[\frac{\partial \vec{v}}{\partial t} + \varepsilon^{-1} (\vec{v} \cdot \vec{\nabla}) \vec{v} \right] = -\vec{\nabla} p - \mathfrak{R}_e^{-1}(\vec{x}) \vec{v}$$

- Fluid transport

$$\varepsilon \frac{\partial C}{\partial t} + \vec{v} \cdot \vec{\nabla} C = \vec{\nabla} \cdot [\mathfrak{D}_e(\vec{x}) \vec{\nabla} C] + R(C, \vec{x}) + S(C, \vec{x})$$

Fluid Dynamics Equations

- Mass balance

$$\vec{\nabla} \cdot (\rho \vec{v}) = S_B$$

- Momentum balance

$$\frac{\rho}{\varepsilon} \left[\frac{\partial \vec{v}}{\partial t} + \varepsilon^{-1} (\vec{v} \cdot \vec{\nabla}) \vec{v} \right] = -\vec{\nabla} p - \Omega_e^{-1}(\vec{x}) \vec{v}$$

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Diffusion in the brain

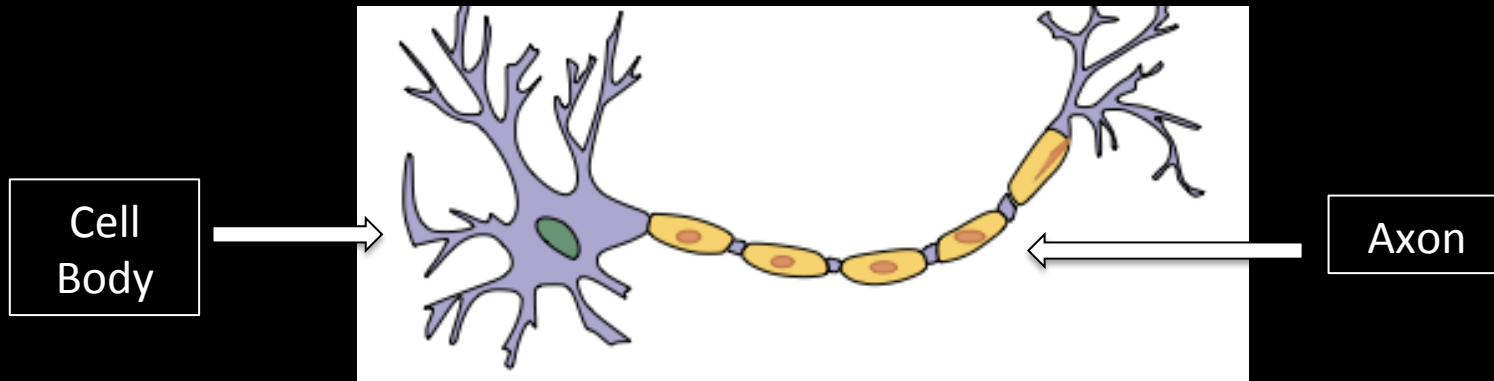


Diffusion in the brain



GRAY MATTER:
NEURON BODIES

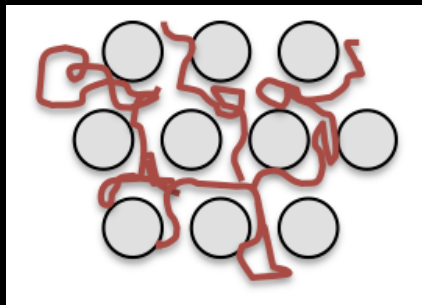
WHITE MATTER:
HIGHLY ALIGNED NEURONAL AXONS



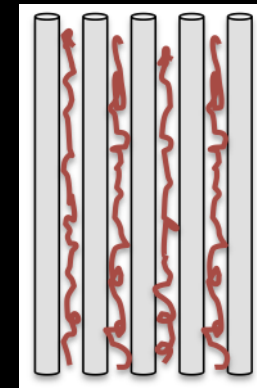
Diffusion in the brain



GRAY MATTER:
NEURON BODIES
ISOTROPIC DIFFUSION



WHITE MATTER:
HIGHLY ALIGNED NEURONAL AXONS
ANISOTROPIC DIFFUSION



Magnetic Resonance Imaging scanner



Thank you!